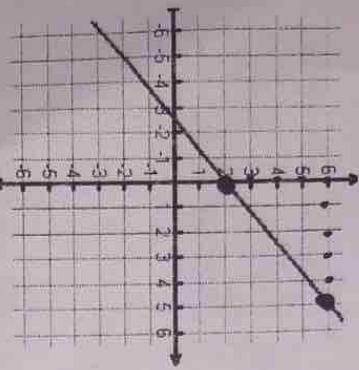


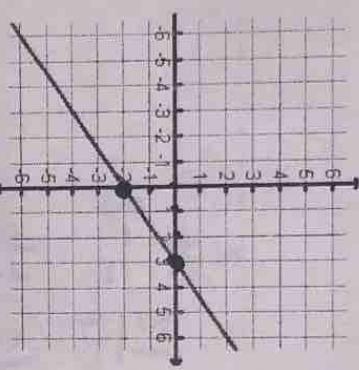
### Writing an equation of a line given a graph.

- Use any 2 "good" points on the graph to find the slope, m.
- Find the y-intercept on the graph, b.
- Substitute slope for m and y-intercept for b into the equation  $y = mx + b$ .

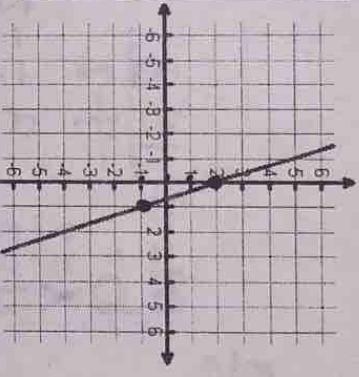
$m = \frac{4}{5}$   $b = 2$   $y = \frac{4}{5}x + 2$



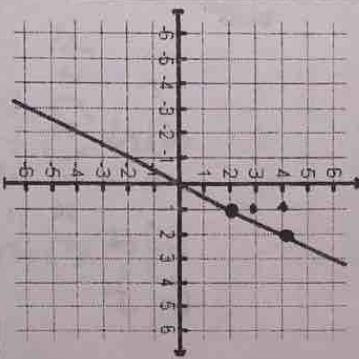
$m = \frac{2}{3}$   $b = -2$   $y = \frac{2}{3}x - 2$



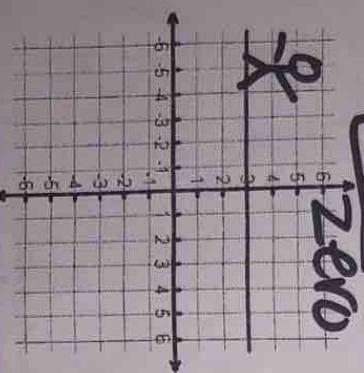
$m = -\frac{3}{2}$   $b = 2$   $y = -\frac{3}{2}x + 2$



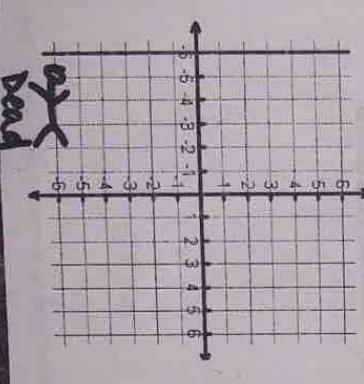
$m = 2$   $b = 0$   $y = 2x$



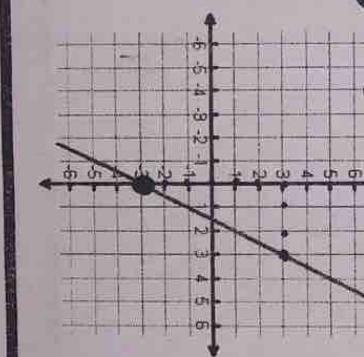
~~$\infty$~~   
zero



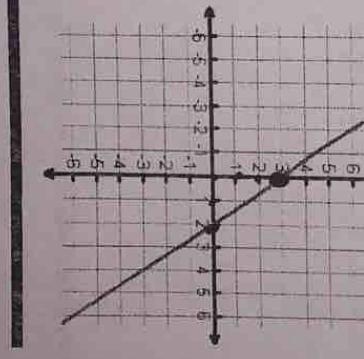
9. undefined  $y = 3$



10. undefined  $x = -10$



11. undefined  $m = 2$   $b = -3$   $y = 2x - 3$



12. undefined  $m = \frac{3}{2}$   $b = 3$   $y = \frac{3}{2}x + 3$

**Writing an equation of a line given m and a point.**

- A. Substitute slope for m and the point (x, y) into  $y=mx+b$  and solve for b.  
 B. Substitute m and b back into the equation.

13.  $m = 2$  and Point: (2, 3)  
 $b = -1$   
 $x = 2$   
 $y = 3$   
 $y = mx + b$   
 $3 = 2(2) + b$   
 $3 = 4 + b$   
 $-4 -4$   
 $b = -1$

$$y = 2x - 1$$

15.  $m = -2$  and Point: (-5, 3)  
 $b =$   
 $x = -5$   
 $y = 3$   
 $y = mx + b$   
 $3 = -2(-5) + b$   
 $3 = 10 + b$   
 $-7 -7$   
 $b = -7$

$$y = -2x - 7$$

17.  $m = \frac{1}{2}$  and Point: (-1, -2)

14.  $m = \frac{1}{2}$  and Point: (4, 2)  
 $b =$   
 $x = 4$   
 $y = -3$   
 $y = \frac{1}{2}x + b$   
 $2 = \frac{1}{2}(4) + b$   
 $2 = 2 + b$   
 $-5 -5$   
 $b = -3$

$$y = \frac{1}{2}x - 3$$

16.  $m = 4$  and Point (1, 4)  
 $b =$   
 $x = 1$   
 $y = 4$   
 $y = 4x + b$   
 $4 = 4(1) + b$   
 $4 = 4 + b$   
 $0 -0$   
 $b = 0$

$$y = 4x$$

19.  $m = 3$  and Point: (3, 0)

20.  $m = \text{undefined}$  and Point (3, 6)

**Writing an equation of a line given TWO points.**

- A. Use the slope formula to find m.  
 B. Pick one point, substitute slope form, the point (x, y) and then solve for b.  
 C. Substitute m and b back into the equation.

21. (2, 3) and (4, 5)  
 $m = 1$   
 $b =$   
 $x = 2$   
 $y = 3$   
 $\frac{5-3}{4-2} = \frac{2}{2} = 1$   
 $3 = 1(2) + b$   
 $3 = 2 + b$   
 $-2 -2$   
 $b = 1$

22. (2, 3) and (-4, 15)  
 $m = -2$   
 $b =$   
 $x = 2$   
 $y = 3$   
 $\frac{15-3}{-4-2} = \frac{12}{-6} = -2$   
 $3 = -2(2) + b$   
 $3 = -4 + b$   
 $b = 7$

23. (2, 2) and (0, 4)

24. (2, 3) and (1, 4)

25. (4, 5) and (5, 2)

- Graphs:
  - o Lines intersect and are in the \_\_\_\_\_ plane.
- Equations:
  - o SAME slopes
  - o \_\_\_\_\_ y-intercepts

Are these lines parallel?

1.  $y = -2x + 1$  and  $y = -2x - 4$

parallel

2.  $y = 3x - 4$  and  $-3x + y = 1$

$$\begin{array}{r} +3x \\ \hline y = 3x + 1 \end{array}$$

Parallel

Writing an Equation of a Line PARALLEL to another and given a point.

- Given equation should be solved for y ( $y = mx + b$ ).
- Write down the slope of that line.
- Substitute m and  $(x, y)$  in  $y = mx + b$ . Solve for b.
- Write the equation using the slope and y-intercept.

3. Write a line parallel to the line  $2x + y = 3$  and passes through the point  $(-2, 5)$ .

$$\begin{array}{r} 2x + y = 3 \\ -2x \\ \hline y = -2x + 3 \end{array}$$

$$\begin{array}{l} m = -2 \\ b = 1 \\ x = -2 \\ y = 5 \end{array}$$

$$\begin{array}{r} 5 = -2(-2) + b \\ -4 = 4 + b \\ b = 1 \end{array}$$

4. Write a line parallel to the line  $y = 3x - 5$  and passes through the point  $(-5, -2)$ .

$$\begin{array}{r} -2 = 3(-5) + b \\ -2 = -15 + b \\ +15 \quad +15 \\ 13 = b \\ y = 3x + 13 \end{array}$$

5. Write a line parallel to the line  $y = -4x + 1$  and passes through the point  $(2, -1)$ .

$$\begin{array}{r} -1 = -4(2) + b \\ -1 = -8 + b \\ +8 \quad +8 \\ b = 7 \\ y = -4x + 7 \end{array}$$

6. Write a line parallel to the line  $y = -x - 7$  and passes through the point  $(-4, -4)$ .

$$\begin{array}{r} -4 = -1(-4) + b \\ -4 = 4 + b \\ -4 \quad -4 \\ b = -8 \\ y = -x - 8 \end{array}$$

## Perpendicular Lines

- Graphs:
  - Lines intersect at a \_\_\_\_\_ angle.

- Equations:
  - ~~slope~~ ~~intercept~~ **OPPOSITE RECIPROCAL**
  - ~~slope~~ ~~intercept~~ **\*change sign AND flip**

**Writing an Equation of a Line PERPENDICULAR to another and given a point.**

- Given equation should be solved for y. ( $y = mx + b$ ).
- Write down the perpendicular slope of that line.
- Substitute the new slope and  $(x, y)$  in  $y = mx + b$ . Solve for b.
- Write the equation using m and b.

7. Write a line **perpendicular** to the line  $y = \frac{1}{2}x - 2$  and passes through the point  $(1, 0)$ .

$$\begin{aligned} m &= -2 & 0 &= -2(1) + b \\ b &= & 0 &= -2 + b \\ x &= 1 & 2 &= b \\ y &= 0 & \boxed{y = -2x + 2} \end{aligned}$$

8. Write a line **perpendicular** to the line  $y = -3x + 2$  and passes through the point  $(6, 5)$ .

$$\begin{aligned} m &= \frac{1}{3} & 5 &= \frac{1}{3}(6) + b \\ b &= & 5 &= 2 + b \\ x &= 6 & 3 &= b \\ y &= 5 & \boxed{y = \frac{1}{3}x + 3} \end{aligned}$$

- \* 9. Write a line **perpendicular** to the line  $2x + 3y = 9$  and passes through the point  $(6, -1)$ .

$$\begin{aligned} m &= \frac{3}{2} & 2x + 3y &= 9 \\ -1 &= \frac{3}{2}(6) + b & 2x &- 2x \\ b &= & 3 &-1 = 9 + b \\ x &= 6 & -9 &-9 \\ y &= -1 & b &= -10 \\ & & \boxed{y = \frac{3}{2}x - 10} & \end{aligned}$$

10. Write a line **perpendicular** to the line  $y = 2x - 1$  and passes through the point  $(2, 4)$ .

$$\begin{aligned} m &= -\frac{1}{2} & 4 &= -\frac{1}{2}(2) + b \\ b &= & 4 &= -1 + b \\ x &= 2 & 5 &= b \\ y &= 4 & \boxed{y = -\frac{1}{2}x + 5} \end{aligned}$$