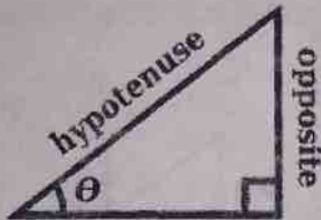
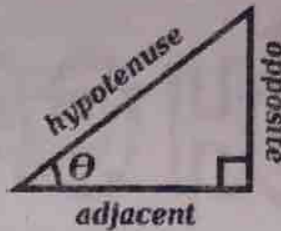


# Right Triangle Trigonometry

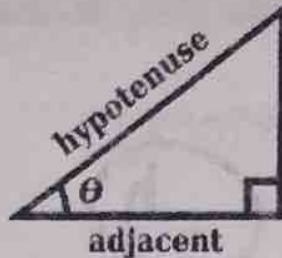


$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

Some

Old

Hippie

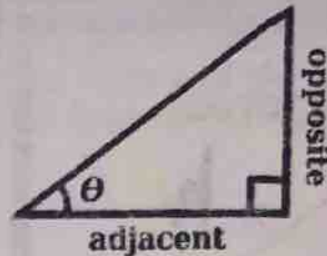


$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

Came

A

Hoppin



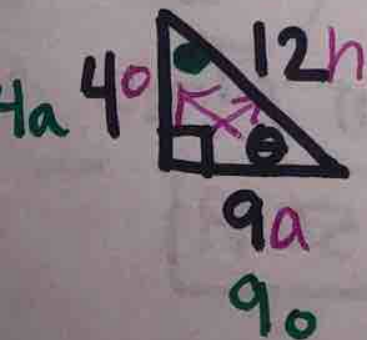
$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

Through

Or

Argument

Copyright: Algebraaurus 2016



$$\sin \theta = \frac{4}{12} = \frac{1}{3}$$

$$\cos \theta = \frac{9}{12} = \frac{3}{4}$$

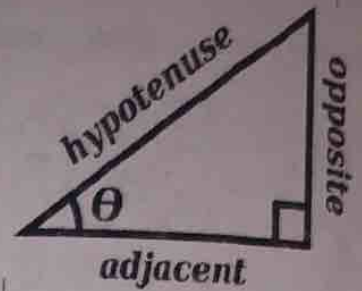
$$\tan \theta = \frac{4}{9}$$

$$\sin(90-\theta) = \frac{9}{12} = \frac{3}{4}$$

$$\cos(90-\theta) = \frac{4}{12} = \frac{1}{3}$$

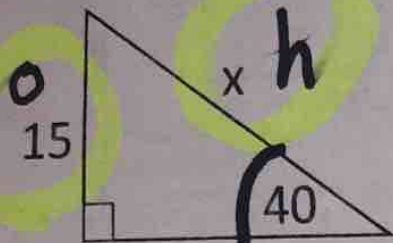
$$\tan(90-\theta) = \frac{9}{4}$$

# Using SOH CAH TOA



Use Sine, Cosine, and Tangent to solve for missing sides or angles in right triangles.

Solve for x.

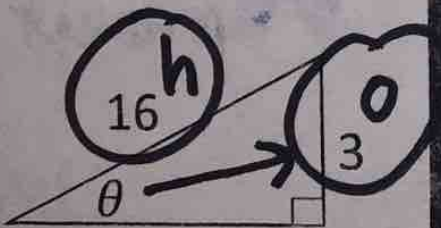


$$\sin 40 = \frac{15}{x}$$

$$x = \frac{15}{\sin 40}$$

$$x = 23.33$$

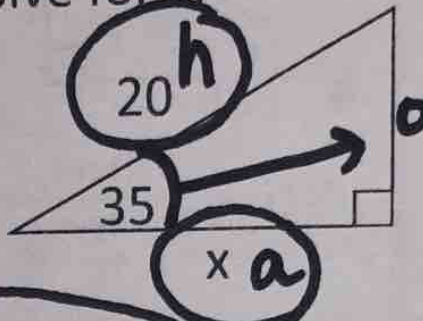
Solve for  $\theta$ .



$$\sin^{-1}\left(\frac{3}{16}\right)$$

$$10.8069$$

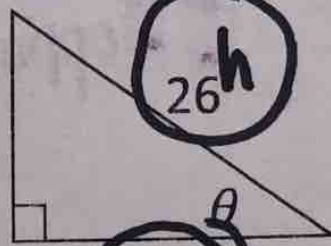
Solve for x.



$$\cos 35 = \frac{x}{20}$$

$$x = 16.38$$

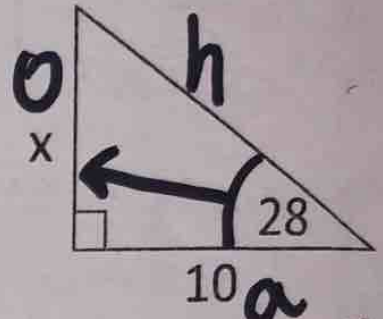
Solve for  $\theta$ .



$$\cos^{-1}\left(\frac{10}{26}\right)$$

$$67.38$$

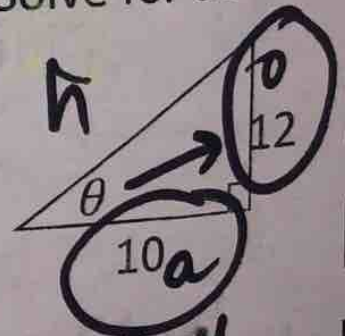
Solve for x.



$$\tan 28 = \frac{x}{10}$$

$$5.32$$

Solve for  $\theta$ .

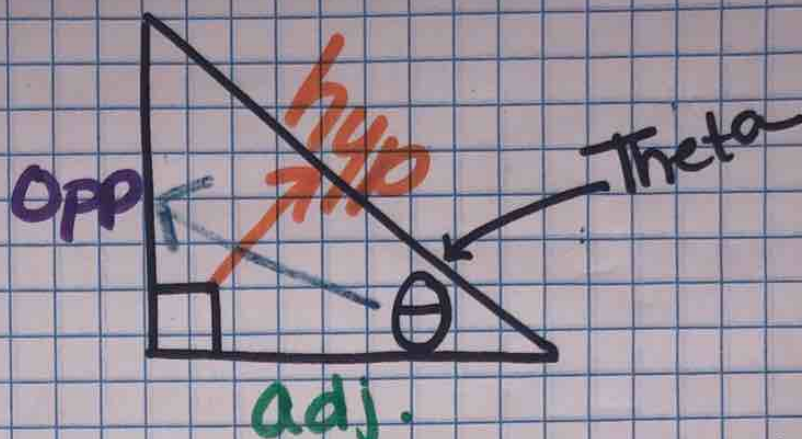


$$\tan^{-1}\left(\frac{12}{10}\right)$$

$$50.19$$



Some  
Old  
Hippie



Came

A

Hoppin

Through

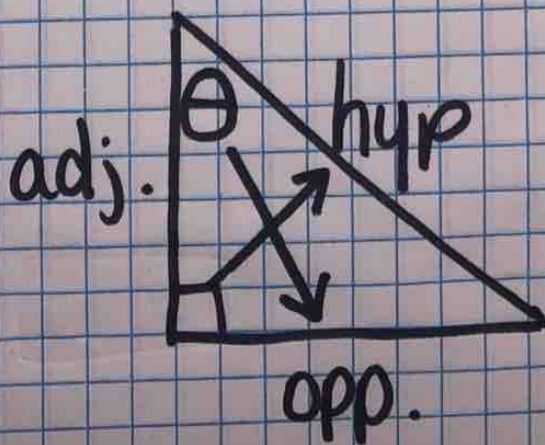
Our

Apartment

### Finding Missing Sides

1. Label  $\Delta$  w/ opp, hyp, adj
2. Circle what you have & what you need
3. Determine which function to use (sine, cosine, tangent)
4. Set up Equation + Solve

\* UP high, multiply  
Down Low, switch & go



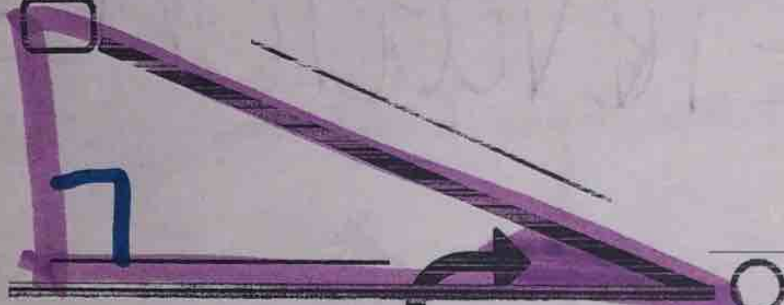


## Angles of Elevation

bottom  
inside

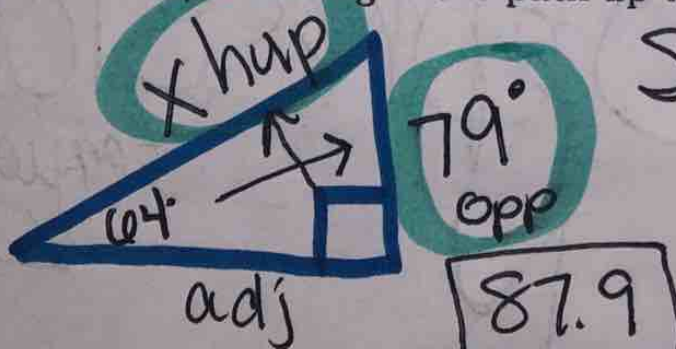
An \_\_\_\_\_ is the angle between the \_\_\_\_\_ and the \_\_\_\_\_ of \_\_\_\_\_ to an object when \_\_\_\_\_.

The \_\_\_\_\_ of \_\_\_\_\_ is the imaginary path that your eyes follow when looking at an object.



angle of elevation

**Example one:** Lisa is standing at the bottom of a hill. The angle of elevation from her to the top of the hill is  $64^\circ$ . If the hill is 79 feet tall, how long is the path up the hill?

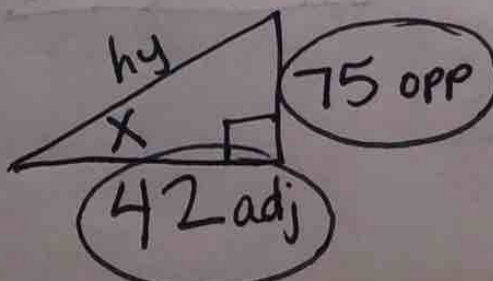


$$\sin 64 = \frac{79}{x}$$

$$x = \frac{79}{\sin 64}$$

$$87.9$$

**Example two:** A deer is standing 42 feet from the base of a 75 foot tall tree. What is the angle of elevation from her to a squirrel sitting on top of the tree?



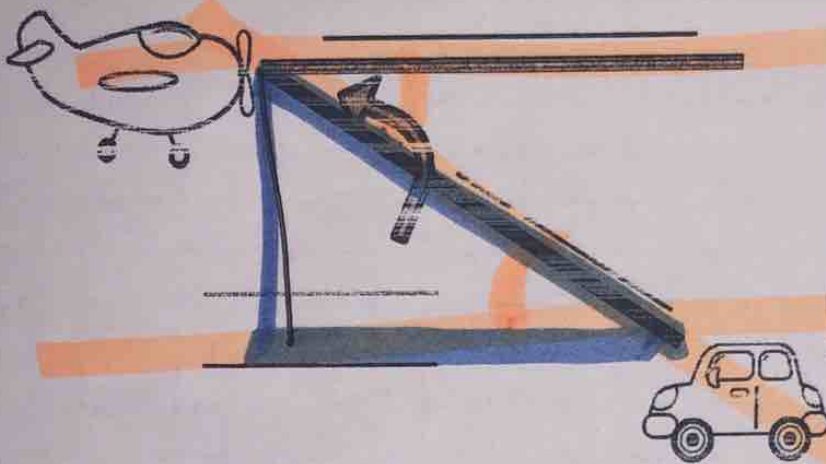
$$\tan^{-1}(75/42)$$

$$60.8^\circ$$

\*OUTSIDE Angles of Depression =  $\angle$  of elevation

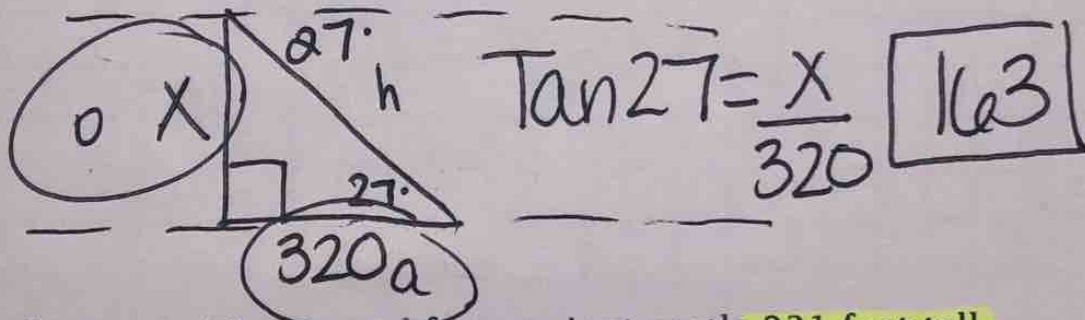
the triangle

An \_\_\_\_\_ is the angle between the \_\_\_\_\_ and the \_\_\_\_\_ of \_\_\_\_\_ to an object when \_\_\_\_\_.

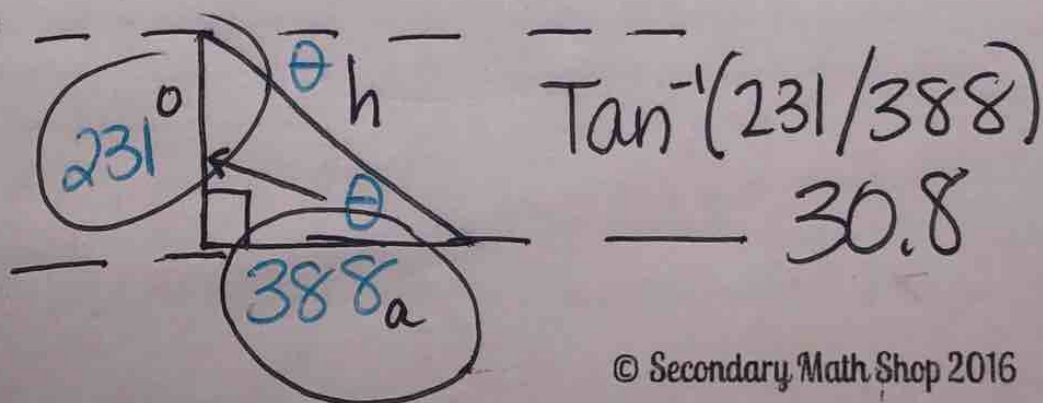


The \_\_\_\_\_ of \_\_\_\_\_ is the imaginary path that your eyes follow when looking at an object.

**Example one:** The angle of depression from a fisherman on top of a cliff to a boat 320 feet from the base of the cliff is  $27^\circ$ . How tall is the cliff?



**Example two:** The tower of an ancient castle **231 feet tall** and casts a **shadow that is 388 feet long**. What is the angle of depression that the sun makes with the ground to create the shadow?



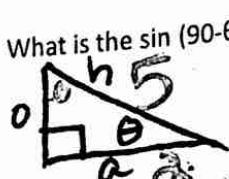
$(90-\theta)$  means other  $\angle$

Guided Practice:

\* Draw Pictures

1. Let  $\cos \theta = \frac{2}{5}$ . What is the  $\sin(90-\theta)$ ?

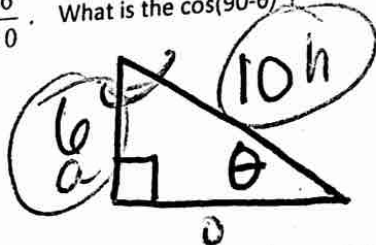
$$\cos \theta = \frac{2}{5} = \frac{a}{h}$$



$$\frac{2}{5}$$

2. Let  $\sin \theta = \frac{6}{10}$ . What is the  $\cos(90-\theta)$ ?

$$\frac{6}{10} = \frac{a}{h}$$

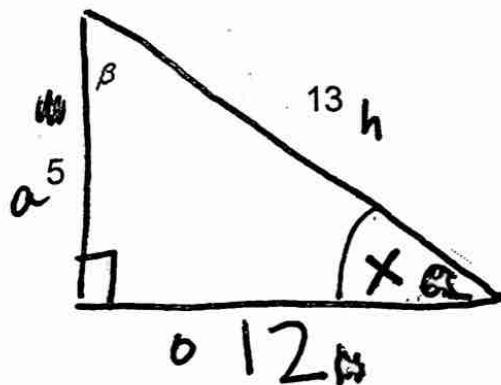


$$\frac{6}{10}$$

3a. Write the trigonometric function for  $\alpha$  represented in the right triangle below.

b. What is the length of the missing leg of the triangle?

$$5^2 + x^2 = 13^2$$



Find the following values:  $\cos \alpha = \frac{12}{13}$   $\tan \alpha = \frac{5}{12}$

$$\sin \beta = \frac{12}{13} \quad \tan \beta = \frac{12}{5} \quad \frac{\sin \beta}{\cos \beta} = \frac{12}{5}$$

4. Given  $\tan \alpha = \frac{7}{24}$ , draw a right triangle that would represent this trigonometric ratio.

Find the following:

$$\sin \alpha = \frac{7}{25}$$

$$\cos \alpha = \frac{24}{25}$$

$$\sin(90-\alpha) = \frac{24}{25}$$

$$\cos(90-\alpha) = \frac{7}{25}$$

